

U is a function of x, i.e. $U = U(x)$

$$\text{If } U = x \rightarrow \frac{dU}{dx} = 1$$

Y	$\frac{dY}{dx}$
U^n	$nU^{n-1} \frac{dU}{dx}$
Trigonometric Functions	
$\sin U$	$\cos U \frac{dU}{dx}$
$\cos U$	$-\sin U \frac{dU}{dx}$
$\sec U$	$\sec U \tan U \frac{dU}{dx}$
$\tan U$	$\sec^2 U \frac{dU}{dx}$
$\csc U$	$-\csc U \cot U \frac{dU}{dx}$
$\cot U$	$-\csc^2 U \frac{dU}{dx}$
Inverse Trigonometric Functions	
$\sin^{-1} U$	$\frac{1}{\sqrt{1-U^2}} \frac{dU}{dx}, U < 1$
$\cos^{-1} U$	$\frac{-1}{\sqrt{1-U^2}} \frac{dU}{dx}, U < 1$
$\tan^{-1} U$	$\frac{1}{1+U^2} \frac{dU}{dx}$
$\cot^{-1} U$	$\frac{-1}{1+U^2} \frac{dU}{dx}$
$\sec^{-1} U$	$\frac{1}{U\sqrt{U^2-1}} \frac{dU}{dx}, U > 1$
$\csc^{-1} U$	$\frac{-1}{U\sqrt{U^2-1}} \frac{dU}{dx}, U > 1$

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Tabulation of Basic integrals

$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$
$\int \frac{dx}{x} = \ln x + C$
$\int e^x dx = e^x + C$
$\int a^x dx = \frac{a^x}{\ln a} + c, \quad a > 0, a \neq 1$
$\int \cos x dx = \sin x + C$
$\int \sin x dx = -\cos x + C$
$\int \sec^2 x dx = \tan x + C$
$\int \csc^2 x dx = -\cot x + C$
$\int \sec x \tan x dx = \sec x + C$
$\int \csc x \cot x dx = -\csc x + C$
$\int \tan x dx = \ln \sec x + C$
$\int \cot x dx = \ln \sin x + C$
$\int \sec x dx = \ln \sec x + \tan x + C$
$\int \csc x dx = \ln \csc x - \cot x + C$

How to Evaluate $\int \sin^m x \cos^n x dx$

If the power of the sine is odd (m is odd) then:

Save one sine factor

Use $\sin^2 x = 1 - \cos^2 x$

Let $U = \cos x$

b) If the power of the cosine is odd (n is odd) then:

Save one cosine factor

Use $\cos^2 x = 1 - \sin^2 x$

Let $U = \sin x$

c) If the powers of both the sine and cosine are odd then:

Use either approach a) or approach b).

d) If the powers of both the sine and cosine are even then:

Use half angle identities: $\sin^2 x = \frac{1}{2}(1 - \cos 2x)$, $\cos^2 x = \frac{1}{2}(1 + \cos 2x)$

$$\sin x \cos x = \frac{1}{2} \sin 2x$$

How to Evaluate $\int \tan^m x \sec^n x dx$

If the power of the tangent is odd then:

Save one factor of $\sec x \tan x$

Use $\tan^2 x = \sec^2 x - 1$

Let $U = \sec x$

b) If the power of the secant is even then:

Save one factor of $\sec^2 x$

Use $\sec^2 x = 1 + \tan^2 x$

Let $U = \tan x$

c) If the power of the tangent is odd and the power of the secant is even then:

Use either approach a) or b).