1. (a) Complete the tables below for the given exponential and logarithmic functions.

$$
y=3^{x} \quad \begin{array}{|c|c|}
\hline x & y \\
\hline-3 & \\
-2 & \\
-1 & \\
0 & \\
1 & \\
2 & \\
3 & \\
5 & \\
\hline
\end{array}
$$

$$
y=\log _{3} x
$$

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
|  | -3 |
|  | -2 |
|  | -1 |
|  | 0 |
|  | 1 |
|  | 2 |
|  | 3 |

(b) Graph these two functions along with $\mathrm{y}=\mathrm{x}$ on the coordinate grid. Include any asymptote(s) and intercept(s).
(c) What do you notice about the tables in part (a)? What do you notice about the graphs?


## Conversions from one form to another

Use
$\log _{a} x=y$
$\leftrightarrow$
$\mathbf{a}^{\mathrm{y}}=\mathbf{x}$
2. Complete the chart, converting the given equation from one form to the other.

| Logarithmic form | Exponential form |
| :--- | :---: |
| (a) $\log _{3} 81=4$ |  |
| (b) $\log 0.001=-3$ | $7^{5}=16,807$ |
| (c) | $\mathrm{e}^{2.9957} \approx 20$ |
| (d) |  |
| (e) $\log _{5} 1=0$ | $12^{1}=12$ |
| (f) |  |
| (g) $\ln 39 \approx 3.6636$ |  |

3. Evaluate without a calculator. Give exact answers, whenever possible. Show your reasoning.
(a) $\log _{2} 64$
(b) $\log 100,000,000$
(c) $\log _{3} 1$

## Calculator Keys:

Common logarithm LOG $=\log _{10} \quad$ Natural logarithm LN $=\log _{\mathrm{e}}$
4. Evaluate. Use your calculator to approximate these to 4 decimal places.
(a) $\log 153$
(b) $\log 0.0005$
(c) $\ln 44$

## Solving logarithmic equations:

Use
(1) changing forms or
(2) $\log _{\mathrm{a}} \mathrm{u}=\log _{\mathrm{a}} \mathrm{v} \quad \leftrightarrow \quad \mathrm{u}=\mathrm{v}$
or (3) $\mathrm{a}^{\mathrm{u}}=\mathrm{a}^{\mathrm{v}} \quad \leftrightarrow \quad \mathrm{u}=\mathrm{v}$
5. Solve for x . Give exact answers, if possible.
(a) $\log _{3} \mathrm{x}=10$
(b) $\mathrm{e}^{2 \mathrm{x}}=5$
(c) $10^{x+3}=10,000,000$

| "Log Rules" |  |
| :---: | :---: |
| 1. $\log _{\mathrm{b}} \mathrm{b}=1$ because $\mathrm{b}^{1}=\mathrm{b}$ | 5. $\log _{b} \mathrm{M} \cdot \mathrm{N}=\log _{b} \mathrm{M}+\log _{b} \mathrm{~N}$ since $b^{M} \cdot b^{N}=b^{M+N}$ |
| 2. $\log _{\mathrm{b}} 1=0$ because $\mathrm{b}^{0}=1$ | 6. $\log _{b} \frac{M}{N}=\log _{b} M-\log _{b} N$ since $\frac{b^{M}}{b^{N}}=b^{M-N}$ |
| 3. $\log _{b} b^{\mathrm{n}}=\mathrm{n}$ because $\mathrm{b}^{\mathrm{n}}=\mathrm{b}^{\mathrm{n}}$ | 7. $\log _{\mathrm{b}} \mathrm{M}^{\mathrm{p}}=\mathrm{p} \cdot \log _{\mathrm{b}} \mathrm{M}$ since $\left(\mathrm{b}^{\mathrm{M}}\right)^{\mathrm{p}}=\mathrm{b}^{\mathrm{M} \cdot \mathrm{p}}$ |
| 4. $\mathrm{b}^{\log _{\mathrm{b}} \mathrm{n}}=\mathrm{n}$ because $\log _{b} \mathrm{n}=\log _{\mathrm{b}} \mathrm{n}$ | 8. $\log _{\mathrm{b}} \mathrm{M}=\frac{\log _{\mathrm{a}} \mathrm{M}}{\log _{\mathrm{a}} \mathrm{b}}$ |

6. Fill in the blanks using the log rules
(a) $\log 3+\log 5=\log$
(b) $\ln 20-\ln 10=\ln$ $\qquad$ (c) $\log _{3} 4^{5}=$ $\qquad$ $\cdot \log _{3} 4$
(d) $8^{\log _{8} 1.25}=$ $\qquad$ (e) $\log 10^{4.5}=$
7. Evaluate. Use your calculator to approximate these to 4 decimal places.
(a) $\log _{2} 16$
(b) $\log _{7} 28$
(c) $\log _{5} 1000$
8. Given that $\log _{10} 2 \approx 0.301$, find each of the following.
(a) $\log _{10} 4$
(b) $\log _{10} 2000$
(c) $\log _{10} 5$
9. How would you enter $\mathrm{y}=\log _{2} \mathrm{x}$ on a graphing calculator?

What about $\mathrm{y}=\log _{5} \mathrm{x}$ ?

## Simple Interest

10. Invest $\$ 1,000$ at $4 \%$ for 3 years. Find the accumulated amount.

## Compound Interest

11. Invest $\$ 1,000$ at $3.5 \%$ compounded $\qquad$ for 5 years. Find the accumulated amount.
(a) monthly
(b) quarterly
(c) continuously
12. The formula $\mathrm{A}=\mathrm{Pe}^{(\mathrm{APR} \cdot \mathrm{Y})}$ gives the accumulated amount ( A ) of an investment when P is the initial investment, APR is the annual interest rate, and Y is the time in years, assuming continuous compounding and no deposits or withdrawals.

For an initial investment of $\$ 2,000$, compounded continuously at a $7 \%$ annual interest rate, find to the nearest tenth of a year when this investment doubles in value.
13. The formula for the accumulated amount, A , of an investment (or loan) is given by the formula, $\mathrm{A}=\mathrm{P}\left(1+\frac{\mathrm{APR}}{\mathrm{n}}\right)^{(\mathrm{n} \cdot \mathrm{Y})}$, where P is the principal, APR is the annual interest rate, and n is the annual number of interest periods, and Y is the number of years.

For an initial investment of $\$ 2,000$, compounded monthly at a $2 \%$ annual interest rate, find to the nearest tenth of a year when this investment doubles in value.
14. For an initial investment of $\$ 1,000$, compounded annually at a $4.5 \%$ annual interest rate, find to the nearest tenth of a year when this investment doubles in value.

Complete the table:

| APR | $3.5 \%$ | $5 \%$ | $7 \%$ | $10 \%$ |
| :---: | :--- | :--- | :--- | :--- |
| $\mathrm{T}_{\text {double }}$ ( (sing 70/P <br> formula) |  |  |  |  |
| $\mathrm{T}_{\text {double }}$ (using log <br> formula) |  |  |  |  |
| Touble <br> (exact, <br> assuming $\mathrm{n}=12$ ) |  |  |  |  |

