## Unit II Journal – Chapters 4 & 9

Name \_\_\_\_\_

Respond to each item, giving sufficient detail. Neatly handwrite your responses. *This should be very helpful to you as you prepare for exams*.

Rule	Example
$a^m \cdot a^n = a^{m+n}$	$5^3 \cdot 5^4 =$
$\frac{a^m}{a^n} = a^{m-n}$	$\frac{8^6}{8^2} =$
$a^0 = 1, a \neq 0$	$10^0 =$
$(a^m)^n = a^m \cdot n$	$(\beta^2)^5 =$
$a^{-n} = \frac{1}{a^n}$	$10^{-2} = $

1. Complete the following exponent rules chart. Show clear use of the properties.

2. The simple interest formula is I = \_\_\_\_\_\_, where P represents the original amount (principal), APR represents the interest rate, and Y represents the time in years.

Calculate the amount of money you have in the following account after 5 years, assuming that you earn simple interest, if you deposit \$1,000 in an account with an annual interest rate of 3.5%. Show your work.

3. The compound interest formula for the accumulated amount of an investment is

$$A = P \left( 1 + \frac{APR}{n} \right)^{(nY)}$$

where P is the starting principal, APR is the \_\_\_\_\_\_ and n is the total number of compounding periods per year. \_\_\_\_\_ is the number of years (which may be a decimal number).

Common numbers of compoundings include 1 for annually, 2 for \_\_\_\_\_,

\_\_\_\_\_ for quarterly, 12 for \_\_\_\_\_\_, \_\_\_\_ for weekly, and 360 (or, sometimes, 365) for \_\_\_\_\_\_.

4. If interest is compounded "continuously" (an infinite number of times each year), we use a new formula for the accumulated amount, A = \_\_\_\_\_\_, where P is the principal, APR is the annual percentage rate, and Y is the number of years.

The number e is (like  $\pi$ ) a transcendental number and is approximately \_\_\_\_\_\_.

Use the compound interest formula to compute the balance for an investment of \$1,500 at an APR of 2.5% for 5 years. Assume continuous compounding. Show your work.

(a) Use the compound interest formula to compute the balance for an investment of \$1,500 at an APR of 4% for 5 years. Assume quarterly compounding. Show your work.

(b) Use the compound interest formula to compute the balance for an investment of \$1,500 at an APR of 4% for 5 years. Assume monthly compounding. Show your work.

(c) Use the compound interest formula to compute the balance for an investment of \$1,500 at an APR of 4% for 5 years. Assume daily compounding. Show your work.

(d)&(e) Then compute the annual percentage yield (APY) for part (a) and part (b). Round to the nearest hundredth of a percent. Show your work.

6. The savings plan formula, with regular payments, is

$$A = PMT \times \frac{\left[ \left( 1 + \frac{APR}{n} \right)^{(n \cdot Y)} - 1 \right]}{\left( \frac{APR}{n} \right)}$$

where A = the accumulated savings plan balance or future value,

PMT = the \_\_\_\_\_ (deposit) amount,

APR = the \_\_\_\_\_ (as a decimal), &

n = \_\_\_\_\_

Y = the number of years

We assume that the initial principal is \$0 before the payments begin.

Find the savings plan balance after 12 months with an APR of 3% and monthly payments of \$150. Show the formula setup and the solution.

7. The total return is the percentage change in the investment value from the original principal, P, to a later accumulated balance, A. Complete the formula below.

Total return = \_\_\_\_\_

The annual return is the annual percentage yield (APY) that would give the same overall growth over Y years. Complete the formula below.

Annual return = \_\_\_\_\_

Compute the annual and total returns for the following scenario: Five years after buying 100 shares of XYZ stock for \$50 per share, you sell the stock for \$7,500. Show your work.

8. An exponential function grows (or decays) by the same amount per unit of time. For any quantity Q growing exponentially with a fractional growth rate r,

Q = \_\_\_\_\_,

where Q = the value of the exponentially growing quantity at time t,

 $Q_0 =$  the \_\_\_\_\_ value of the quantity (at t = 0),

r = the fractional growth rate (which may be positive or negative) for the quantity, &

t = time

Negative values of r correspond to exponential decay; positive values of r correspond to exponential \_\_\_\_\_\_\_. The units of time used for t and r must be the same. For example, if the growth rate is 5% per month, then t must also be measured in months; if the growth rate is 5% per year, then t must be measured in \_\_\_\_\_\_.

A city's population starts at 100,000 people and grows 5% per year.

(a) What is the general formula for the population growth of this city?

Q = \_\_\_\_\_

(b) Then find the population 7 years later. Round to the nearest person. Show your work.

9. Start with the general equation,  $Q = Q_0(1 + r)^t$ .

Substituting  $Q = 2Q_0$  and  $t = T_{double}$ , we have  $2Q_0 = Q_0(1 + r)^{T_{double}}$ .

Dividing both sides by  $Q_0$ , we have  $2 = (1 + r)^{T_{double}}$ .

Raising both sides to the power  $1/T_{double}$ , we have  $2^{1/T_{double}} = 1 + r$ .

Then substituting the expression for 1 + r into the general equation, we have

 $Q = Q_0 \times (2^{1/T_{double}})^t =$ \_\_\_\_\_.

This formula is used when the initial amount,  $Q_0$ , is known and the time it takes for the amount to double,  $T_{double}$ , is also known.

A city's population starts at 100,000 people and doubles every 14 years.

(a) What is the general formula for the population growth of this city?

Q = \_\_\_\_\_ × 2------

(b) Then find the population 7 years later. Round to the nearest person.

A similar formula is used when the initial amount,  $Q_0$ , is known and the time it takes for the amount to halve,  $T_{half}$ , is also known.

 $Q = Q_0 \times \left(\frac{1}{2}\right)^{t/T_{half}}$  We will revisit both of these alternative formulas in Section 8B.

10. Write a few sentences describing something you learned that was new for you in class this unit. You may include a favorite activity, an interesting application, a teaching and learning technique, or a specific concept that you better understand as a result of this unit.

Do your best! Rise to the challenge! Live and learn!